Geometry A 4.1 Angles of Triangles

1. Find $m \angle T$.

2. Find the measures of the numbered angles.


ASSIGNMENT
Name
Hour $\qquad$ Date $\qquad$
2. Find the measures of the missing angles.

4. Find the measures of the numbered angles.

5. Find the measures of the numbered angles.

6. Find $m \angle 1$

7. Find $x$.

8. Find $x$.


## Review:

9. Suppose $\angle 1$ and $\angle 2$ are vertical angles. If $m \angle 1=4 x+2$ and $m \angle 2=8 x-14$, find $m \angle 2$.
10. Suppose $R$ is between $Y$ and $W$. If $R Y=3 x-10, R W=66$, and $Y W=5 x+6$, find $R Y$.

Geometry A
4.2 Congruent Triangles

Name $\qquad$
ASSIGNMENT
Hour Date

1. If $\Delta R T Y \cong \triangle K N B$ complete each pair of congruent parts:
$\angle R \cong$ $\qquad$
$\qquad$

$$
\cong \angle N
$$

$$
\angle Y \cong
$$

$\qquad$

$$
\overline{R T} \cong
$$

$\qquad$
$\overline{R Y} \cong$ $\qquad$

$$
\cong \overline{N B}
$$

Identify the congruent triangles in each diagram.
2.

$\Delta S Q P \cong$ $\qquad$
3.

$\triangle M N O \cong$ $\qquad$
4.

$\triangle E F D \cong$ $\qquad$
5.

$\Delta R V T \cong$ $\qquad$
6. Using the diagram on the right, identify each pair of congruent parts:
$\qquad$ $\angle T \cong$ $\qquad$ $\angle T V R \cong$ $\qquad$
$\overline{R T} \cong$ $\qquad$

$$
\overline{T V} \cong
$$

$\overline{V R} \cong$ $\qquad$


## Review:

For \#7-10, select the property, definition, postulate, or theorem from the box below that justifies each statement. Write the property, definition, postulate, or theorem on the line provided.

| reflexive property | subtraction property | distributive property |
| :--- | :--- | :--- |
| symmetric property | multiplication property | midpoint theorem |
| transitive property | division property | definition of an angle bisector |
| addition property | substitution property | vertical angles theorem |
| segment addition postulate | angle addition postulate | complement theorem <br> supplement theorem |
|  |  |  |

7. If $m \angle 4=m \angle 5$, then $m \angle 4+20=m \angle 5+20$
8. $\mathrm{AD}=\mathrm{AD}$
9. If $\overline{A B} \cong \overline{B C}$ and $\overline{B C} \cong \overline{C E}$, then $\overline{A B} \cong \overline{C E}$
10. If $3(x+2)=60$, then $3 x+6=60$

Geometry A
4.3 Proving Congruence

Name $\qquad$
Hour $\qquad$ Date $\qquad$
ASSIGNMENT

## What household appliance will never be able to swim?

To find out, identify whether each pair of triangles is congruent by SSS, SAS, or ASA. Circle the letter that represents this characteristic. Place the circled letters in the blanks at the bottom of the page above the corresponding problem numbers.
1.


(O) SSS
(T) SAS
(L) ASA
2.

(H) SSS
(K) SAS
(M) ASA
3.


(Y) SSS
(B) SAS
(E) ASA

5.

(S) SSS
(A) SAS
(C) ASA
(J) SSS
(I) SAS
(T) ASA
6.


(W) SSS
(R) SAS
(N) ASA
7.

(K) SSS
(M) SAS
(F) ASA

$$
\overline{1} \frac{}{2} \quad \frac{}{4} \quad \frac{}{5} \frac{-}{6}
$$

Identify whether each pair of triangle are congruent by SSS, SAS, ASA, AAS or HL. Otherwise, write "not enough information."

2.

4.

5.

6.

8.

9.

10.


Geometry A

### 4.4 Triangle Congruence Proofs

Name
Hour $\qquad$

## ASSIGNMENT

1. Given: $\overline{R S} \cong \overline{T S}, V$ is the midpoint of $\overline{R T}$

Prove: $\Delta R S V \cong \Delta T S V$


| Statements | Reasons |
| :--- | :--- |
| 1. $\overline{R S} \cong \overline{T S}$ | 1. |
| 2. | 2. Given |
| 3. | 3. Midpoint Theorem |
| 4. $\overline{V S} \cong \overline{V S}$ | 4. |
| 5. $\Delta R S V \cong \triangle T S V$ | 5. |

2. Given: $\overline{J K} \cong \overline{M K}, \angle N \cong \angle L$ Prove: $\triangle J K N \cong \triangle M K L$


| Statements | Reasons |
| :--- | :--- |
| 1. $\overline{J K} \cong \overline{M K}$ | $\mathbf{1 .}$ |
| 2. $\angle N \cong \angle L$ | 2. |
| 3. $\angle J K N \cong \angle M K L$ | 3. |
| 4. $\triangle J K N \cong \triangle M K L$ | 4. |

3. Given: $\overline{Q R} \| \overline{T U}, S$ is the midpoint of $\overline{Q T}$ Prove: $\overline{R S} \cong \overline{U S}$


| Statements | Reasons |
| :--- | :--- |
| 1. | 1. Given |
| 2. $\angle Q \cong \angle T$ | 2. |
| 3. $S$ is the midpoint of $\overline{Q T}$ | 3. |
| 4. | 4. Midpoint Theorem |
| 5. | 5. Vertical Angles Theorem |
| 6. $\Delta Q S R \cong \triangle T S U$ | 6. |
| 7. $\overline{R S} \cong \overline{U S}$ |  |

4. Given: $\angle D \cong \angle F, \overline{G E}$ bisects $\angle D E F$

Prove: $\overline{D G} \cong \overline{F G}$


| Statements | Reasons |
| :--- | :--- |
| 1. $\angle D \cong \angle F$ | 1. |
| 2. $\overline{G E}$ bisects $\angle D E F$ | 2. |
| 3. | 3. Definition of Angle Bisector |
| 4. | 4. Reflexive Property |
| 5. | $\mathbf{5 .}$ |
| 6. $\overline{D G} \cong \overline{F G}$ | 6. |

## Geometry A

4.5 Isosceles and Equilateral Triangles

Name $\qquad$
ASSIGNMENT

Classify each triangle as scalene, isosceles, or equilateral.
1.

2.

3.

4.

5.

6.

7. Suppose that $\overline{F J} \cong \overline{F H}$ and $\overline{H F} \cong \overline{H G}$. If $m \angle F H G=126^{\circ}$, find $m \angle J$.

$m \angle J=$ $\qquad$
8. Find the value of $y$ and the measure of each side of isosceles $\triangle A B C$ if $A B=B C, A B=4 y, B C=3 y+2$, and $A C=3 y$. Show all organized work.

$$
y=
$$

$\qquad$ $A B=$ $\qquad$ $B C=$ $\qquad$ $A C=$ $\qquad$
9. Find the value of $x$ and the measure of each side of equilateral $\triangle A B C$ if $A B=3 x-2, B C=2 x+4$, and $C A=x+10$. Show all organized work.

$$
x=
$$

$\qquad$ $A B=$ $\qquad$ $B C=$ $\qquad$ $C A=$ $\qquad$
10. Find the value of $x$ and the measure of each side of equilateral $\Delta R S T$ if $R S=2 x+2, S T=3 x$, and $T R=5 x-4$. Show all organized work.

$$
x=
$$

$\qquad$ $R S=$ $\qquad$ $S T=$ $\qquad$ $T R=$ $\qquad$
11. Suppose $\Delta J K M$ is isosceles with vertex angle $K$. If $J K=5 x-3, J M=3 x+7$, and $K M=2 x+9$, find the value of $x, J K, J M$, and $K M$.

$$
x=\square \quad J K=\square \quad J M=\square \quad K M=
$$

12. Given: $\triangle M P R$ is isosceles with vertex $P$, $\overline{P N} \perp \overline{M R}$

Prove: $\overline{M N} \cong \overline{N R}$


| 1. $\triangle M P R$ is isosceles with vertex $P$ | 1. |
| :--- | :--- |
| 2. $\overline{P N} \perp \overline{M R}$ | 2. |
| 3. $\overline{M P} \cong \overline{R P}$ | 3. |
| 4. $\overline{P N} \cong \overline{P N}$ | 4. |
| 5. $\triangle M P N \cong \triangle R P N$ | 5. |
| 6. $\overline{M N} \cong \overline{N R}$ | 6. |

## Review:

13. Find the value of $y$ in the figure at the right.


## Multiple Choice:

14. Given: $m \angle A+m \angle B=150$.

Conjecture: $\angle A$ and $\angle B$ are both acute angles.
Which one of the following is a counterexample to the conjecture?
A. $m \angle A=100$ and $m \angle B=50$
B. $m \angle A=45$ and $m \angle B=105$
C. $m \angle A=65$ and $m \angle B=85$
D. None of the above statements is a counterexample because the conjecture is true.
15. Which one of the following pairs of slopes are slopes corresponding to perpendicular lines?
A. $\frac{2}{3}$ and $\frac{9}{6}$
B. $-\frac{12}{8}$ and $-\frac{3}{2}$
C. $-\frac{2}{3}$ and $\frac{12}{8}$
D. $\frac{10}{15}$ and $-\frac{3}{2}$

Geometry A
Unit 4 Review

Name $\qquad$
Hour $\qquad$
2. Find the measure of each indicated angle.

$m \angle 1=$ $\qquad$ $m \angle 2=$ $\qquad$
3. Find the measure of each indicated angle.

$m \angle 1=$ $\qquad$ $m \angle 2=$ $\qquad$ $m \angle 3=$ $\qquad$ $m \angle 1=$ $\qquad$ $m \angle 2=$ $\qquad$ $m \angle 3=$ $\qquad$
5. Find the measure of each indicated angle.

$m \angle 1=$ $\qquad$ $m \angle 2=$ $\qquad$ $m \angle 3=$ $\qquad$ $m \angle 4=$ $\qquad$ $m \angle 5=$ $\qquad$
6. Refer to the figure below. Find the measure of each indicated angle if $m \angle 6=51^{\circ}$ and $m \angle 8=134^{\circ}$.

$m \angle 1=$ $\qquad$ $m \angle 2=$ $\qquad$ $m \angle 3=$ $\qquad$ $m \angle 4=$ $\qquad$ $m \angle 5=$ $\qquad$
$m \angle 7=$ $\qquad$ $m \angle 9=$ $\qquad$ $m \angle 10=$ $\qquad$ $m \angle 11=$ $\qquad$ $m \angle 12=$ $\qquad$
7. Find the value of $x, A B, B C$, and $A C$ if $\triangle A B C$ is equilateral.

$x=$ $\qquad$

$$
A B=
$$

$\qquad$

$$
B C=
$$

$$
A C=
$$

8. Find the value of $x$.

9. Suppose $\triangle J K M$ is isosceles with vertex angle $K$. If $m \angle J=8 x-5$ and $m \angle M=3 x+25$, find $m \angle K$.
10. Suppose that $\overline{A B} \cong \overline{D B}$ and $\overline{C D} \cong \overline{B D}$. If $m \angle A=31^{\circ}$, find $m \angle B D C$.

$\qquad$
11. Identify the congruent triangles in the figure below.

Then name the corresponding congruent angles and congruent sides for the congruent triangles.

| $\Delta F G D \cong$ |  |
| :--- | :--- |
| $\angle F G D \cong$ | $\overline{D G} \cong$ |
| $\angle G D F \cong$ | $\overline{F D} \cong$ |
| $\angle D F G \cong$ | $\overline{F G} \cong$ |

14. Identify the congruent triangles in the figure below.


Then name the corresponding congruent angles and congruent sides for the congruent triangles.

15. Determine whether you can prove that each pair of triangles is congruent by using $\boldsymbol{S S S}, \boldsymbol{S A S}, \boldsymbol{A S A}, \boldsymbol{A A S}$, or $\boldsymbol{H L}$. If it is not possible to prove that the triangles are congruent, write not possible.
a.

b.


e.

f.

g.

j.

h.

k.

i.

1.

16. Given: $\overline{B D}$ bisects $\angle A B C$
$\overline{A B} \cong \overline{C B}$
Prove: $\triangle B D A \cong \triangle B D C$


| Statements | Reasons |
| :--- | :--- |
| 1. | 1. |
| 2. | 2. |
| 3. | 3. |
| 4. | 4. |
| 5. | 5. |

17. Given: $\angle A \cong \angle C$ $\angle A D B \cong \angle C B D$
Prove: $\triangle A D B \cong \triangle C B D$


| Statements | Reasons |
| :--- | :--- |
| 1. | 1. |
| 2. | 2. |
| 3. | 3. |
| 4. | 4. |

18. Given: $P$ is the midpoint of $\overline{N S}$
$\angle N \cong \angle S$ $\angle M P N \cong \angle R P S$
Prove: $\overline{M N} \cong \overline{R S}$


| Statements | Reasons |
| :--- | :--- |
| 1. | 1. |
| 2. | 2. |
| 3. | 3. |
| 4. | 4. |
| 5. | 5. |
| 6. | 6. |

19. Complete the following proof.

Given: $\overline{A B} \| \overline{D E}$ $\overline{A D}$ bisects $\overline{B E}$

Prove: $\overline{A C} \cong \overline{D C}$


| Statements | Reasons |
| :--- | :--- |
| 1. | 1. |
| 2. | 2. |
| 3. | 3. |
| 4. | 4. |
| 5. | 5. |
| 6. | 6. |
| 7. | 7. |

20. Complete the following proof.

Given: $\overline{A E} \cong \overline{C F}$
$\triangle A B C$ is isosceles with vertex angle $\angle B$.

Prove: $\overline{B E} \cong \overline{B C}$


| Statements | Reasons |
| :--- | :--- |
| 1. $\overline{A E} \cong \overline{C F}$ | 1. |
| 2. $\triangle A B C$ is isosceles with vertex angle $\angle B$. | 2. |
| 3. | 3. Definition of an Isosceles Triangle |
| 4. $\angle A \cong \angle C$ | 4. |
| $5 . \triangle A B E \cong \triangle C B F$ | 5. |
| 6. | 6. |

